

## EE 310 - LAB 4

### Question:

a) The following state space model is given;

$$\begin{aligned} \dot{x} &= Ax + bu & y &= C^T x + du \\ \dot{x} &= \begin{bmatrix} 0 & -2 \\ 2 & -k \end{bmatrix} x + \begin{bmatrix} 0 \\ 4 \end{bmatrix} u & y &= [1 \quad 0]x \end{aligned} \quad (1)$$

In order to obtain the transfer function, the following formula will be used:

$$G(s) = C^T (sI - A)^{-1} b + d \quad (2)$$

By using equation (2) for the state space model in (1), we have;

$$G(s) = \frac{-8}{s^2 + ks + 4} \quad (3)$$

Verify equation (3) by hand calculation.

b) We observe that we found a second-order lag transfer function. Hence, we should compare the following:

$$s^2 + 2D\omega_n s + \omega_n^2 = s^2 + ks + 4 \quad (4)$$

From equation (4), we can obtain the following:

$$\begin{aligned} \omega_n &= 2 \\ D &= \frac{k}{4} \end{aligned} \quad (5)$$

Verify the results in (5) by hand calculation.

- c) When  $D \geq 1$ , there are no oscillations. Hence  $k \geq 4$ . Apply Simulink solution to this problem.
- d) When  $0 < D < 1$ , we have decreasing oscillations. Hence  $0 < k < 4$ . Apply Simulink solution to this problem.
- e) When  $D < 0$ , we have increasing oscillations. Hence  $k < 0$ . Apply Simulink solution to this problem.